High-dimensional machine learning to predict hospital readmission among older people with chronic kidney disease: abridged secondary publication

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- 1. A novel factorisation-based machine-learning model, which is Hong Kong-weighted with fuzzy partition, is proposed to predict the risk of hospital readmission among patients with chronic kidney disease.
- 2. This is one of the first machine-learning models for readmission prediction based on territorywide data in Hong Kong.
- 3. Application of this model may help reduce the cost of hospital management and improve the quality of life among patients with chronic kidney disease.

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Introduction

Over 20% of older people experience unexpected readmission to accident and emergency department within 1 month of discharge. Identifying at-risk patients is important in geriatric medical care planning. However, in older people with multiple chronic diseases, traditional screening methods or basic machine-learning algorithms are difficult to identify disease risk patterns. We developed a Hong Kong-weighted factorisation machine with fuzzy partition (wFMFP) to predict the risk of readmission among patients with chronic kidney disease (Fig 1).

Methods

A total of 418305 admission records of 19457 older patients aged \geq 65 years with chronic kidney disease as the primary diagnosis between 2008 and 2017 in Hong Kong public hospitals were retrieved. Of the 418305 admission records, 392863 (12046 patients) were within 30 days of previous discharge to home. Of the 12046 patients, 4523 (37.55%) had a single readmission and 7523 (62.45%) had multiple readmissions. Data collected included age, district of residence, admission specialty (medicine or clinical oncology), length of stay (LOS), source of admission (emergency department, other hospital, or others), triage category at the emergency department (critical, emergency, urgent, semi-urgent, nonurgent), subacute care (yes or no), LOS of the subacute care, total quantity of drug dispensed, and total prescribed dispensing duration (days).

Among 12046 patients readmitted within

30 days, the mean patient age was 72.35 years; the mean LOS was 1.4360 days; the mean total quantity of drug dispensed was 14.4189 doses; and the mean total prescribed dispensing duration was 8.7560 days. There were 386 362 admissions to medicine specialties and 51 admissions to oncology specialties. The most common triage category at emergency departments was urgent (42.05%), followed by semi-urgent (26.07%), emergency (17.78%), non-urgent (13.48%), and critical (0.62%). The mean LOS of sub-acute care was 17.5550 days. The mean haemoglobin A1c was 52.5285 mmol/mol.

Factorisation machines provide a general predictor that can efficiently model high-order interactions among explanatory features in linear time complexity.¹ Matrix factorisation decomposes a matrix into matrices. Tensor factorisation is the highorder extension of matrix factorisation; it enables modelling of heterogeneous and multidimensional data.² Matrix and tensor factorisations can extract the latent components to enhance data-mining tasks. In this project, CANDECOMP/PARAFAC factorisation was used for prediction. The admission count was used to construct tensors in the proposed models, and non-negative tensor factorisation methods using generalised Kullback-Leibler divergence and multiplicative update rules were followed.^{2,3}

Traditional regression methods usually add clinical attributes as independent variables, ignoring the high-dimensional interrelations and high-order interactions between clinical attributes and diseases. Tensor factorisation provides a powerful framework to model such multi-aspect data by explicitly exploiting the high-dimensional structure to identify latent clusters of data.^{2,3} In this project, we used tensor factorisation to evaluate the risks of all chronic diseases. For each patient, tensor factorisation produced a ranked list of chronic diseases according to predicted risk scores. Risk scores for different diseases in such a rank were used as predictors in a traditional machine-learning model to predict the risk of readmission within a certain period (30 days, 90 days, 1 year).

In the wFMFP model, step 1 is to initialise the number of clusters (equal to the number of sub-wFM models) and the overlap parameter η for training data segmentation. Step 2 is to use fuzzy c-means to obtain membership μ is, cluster centres β_{α} in (1), and the spread width δ_q^q in (2). Step 3 is to repeat step 2 when the stop criterion is not satisfied; otherwise, continue to step 4. Step 4 is to obtain training subsets Ds in (3) according to the generated centres and the spread width through fuzzy c-means. Step 5 is to construct sub-wFM prediction models. Step 6 is to generate the overall prediction output of wFMFP by using (4) with fuzzy weighting mechanism in (5).

$$\mu_{is} = \frac{\left(1/||\vec{x}_{i} - \vec{\beta}_{s}||^{2}\right)^{1/(z-1)}}{\sum_{s=1}^{S} \left(1/||\vec{x}_{i} - \vec{\beta}_{s}||^{2}\right)^{1/(z-1)}}, \quad \vec{\beta}_{s} = \frac{\sum_{i=1}^{N} \mu_{is}^{z} \vec{x}_{i}}{\sum_{i=1}^{N} \mu_{is}^{z}}.$$
(1)

$$\delta_s^q = \sqrt{\frac{\sum_{i=1}^N \mu_{is}^z ||x_i^q - x_s^q||^2}{\sum_{i=1}^N \mu_{is}^{\tilde{z}}}}, \ q = 1, 2, \cdots, Q \ \text{and} \ s = 1, \cdots, S.$$

$$\mathcal{D}_{s} = \{X_{s}, Y_{s}\} = \{(\vec{x}_{i}, y_{i}) | \beta_{s}^{q} - \eta \delta_{s}^{q} \le x_{i}^{q} \le \beta_{s}^{q} + \eta \delta_{s}^{q}\}, \ s = 1, \cdots, S$$
(3)
$$\hat{y}(\vec{x}_{i}) = \frac{\sum_{s=1}^{S} \omega_{s}(\vec{x}_{i}) \cdot wFM_{s}(\vec{x}_{i})}{\sum_{s=1}^{S} \omega_{s}(\vec{x}_{i})}, \ i = 1, 2, \cdots, N.$$
(4)
$$\omega_{s}^{q}(x_{i}^{q}) = \max\left(\min\left(\frac{x_{i}^{q}(\beta_{s}^{q} - \eta \delta_{s}^{q})}{\beta_{s}^{q} - (\beta_{s}^{q} - \eta \delta_{s}^{q})}, \frac{(\beta_{s}^{q} + \eta \delta_{s}^{q}) - x_{i}^{q}}{(\beta_{s}^{q} + \eta \delta_{s}^{q}) - \beta_{s}^{q}}\right), 0\right)$$

$$i = 1, 2, \cdots, N, q = 1, 2, \cdots, Q, s = 1, 2, \cdots, S$$
(5)

$$i=1,2,\cdots,N, q=1,2,\cdots,Q, s=1,2,\cdots,S$$

Performance of wFMFP and other models (factorisation machine with fuzzy partition, factorisation machine, polynomial kernel-based support vector machine, sigmoid kernel-based support vector machine, radial basis function kernel-based support vector machine, and multilayer perceptron) was evaluated by coefficient of determination (R²), mean squared error, mean absolute error, mean absolute percentage error, and median absolute percentage error. Higher R² and lower mean squared error, mean absolute error, mean absolute percentage error, and median absolute percentage error indicate better performance of prediction.

Results

Correlation analysis between readmission variables is shown in Fig 2. wFPFM outperformed other







models in predicting readmission risk when the number of training subsets was >5 (Table).

Discussion

(2)

The wFMFP can deal with the boundary effects and data sparsity issue. In the present study, the wFMFP was superior to other models in predicting readmission risk of patients with chronic kidney disease. The wFMFP can be used as an integral component of the decision support system to better characterise, forecast, and provide preventive

TABLE. Performance of weighted factorisation machine with fuzzy partition (wFMFP) and other machine-learning models in predicting the risk of hospital readmission among patients with chronic kidney disease

| Model | R ² | Mean squared error | Mean absolute error | Mean absolute percentage error | Median absolute percentage error |
|-----------------------------------------------------------------|----------------|--------------------------|---------------------------|-----------------------------------------|-------------------------------------------|
| wFMFP | | | | | |
| 3 wFMs | 0.8267 | 0.2764 | 0.2692 | 0.2458 | 2521 |
| 4 wFMs | 0.8518 | 0.2256 | 0.2263 | 0.2390 | 0.2338 |
| 5 wFMs | 0.8865 | 0.2181 | 0.2411 | 0.2311 | 0.2130 |
| 6 wFMs | 0.8762 | 0.2512 | 0.2142 | 0.2265 | 0.2286 |
| 7 wFMs | 0.8336 | 0.2292 | 0.2295 | 0.2389 | 0.2421 |
| 8 wFMs | 0.8349 | 0.2277 | 0.2221 | 0.2459 | 0.2333 |
| 9 wFMs | 0.8101 | 0.2305 | 0.2322 | 0.2474 | 0.2605 |
| 10 wFMs | 0.7758 | 0.2471 | 0.2302 | 0.2528 | 0.2747 |
| Factorisation machine with fuzzy partition | | | | | |
| 3 FMs | 0.7947 | 0.2633 | 0.2593 | 0.2836 | 0.2994 |
| 4 FMs | 0.8019 | 0.2773 | 0.2667 | 0.2787 | 0.2856 |
| 5 FMs | 0.8249 | 0.2628 | 0.2584 | 0.2924 | 0.3172 |
| 6 FMs | 0.8383 | 0.2649 | 0.2854 | 0.2833 | 0.3174 |
| 7 FMs | 0.8052 | 0.2734 | 0.2621 | 0.2881 | 0.3130 |
| 8 FMs | 0.8495 | 0.2624 | 0.2973 | 0.2856 | 0.3127 |
| 9 FMs | 0.7942 | 0.2735 | 0.3133 | 0.3000 | 0.3245 |
| 10 FMs | 0.7538 | 0.2863 | 0.2973 | 0.3158 | 0.3182 |
| Weighted factorisation machine | 0.8318 | 0.2368 | 0.2656 | 0.2916 | 0.3276 |
| Factorisation machine | 0.7966 | 0.2490 | 0.2931 | 0.2984 | 0.3105 |
| Polynomial kernel-based support vector machine | 0.7718 | 0.2948 | 0.3172 | 0.2934 | 0.3123 |
| Sigmoid Kernel-based support vector machine | 0.7348 | 0.2817 | 0.3291 | 0.2942 | 0.3027 |
| Radial basis function kernel-based support vector machine | 0.7943 | 0.2771 | 0.3012 | 0.2987 | 0.3120 |
| Multilayer perceptron | 0.7943 | 0.2771 | 0.3012 | 0.2987 | 0.3220 |

guideline for readmission risk management. The wFMFP can be used for assessment of discharge and readmission risk. Outcomes from wFMFP can provide a prediction of the explicit risk factors of each patient, which helps decide the disease management strategy such as discharge or intensive

medical care for a certain disease. Implementation of predictive readmission analytics provides hospitals an easy-to-use readmission management tool for healthcare cost reduction, efficiency improvement, and lowering LOS deviation. For patients, the model can assist in the domestic care and provide guidance in lifestyle. For example, patients with high risk of readmission because of diabetes should pay attention to daily glucose control. In addition, the wFMFP can be extensively used in various prediction and classification tasks in other domains (transportation, finance).

We plan to examine the prediction performance differences of wFMFP with different weighted strategies, especially when we assign weights through clustering algorithms. We also plan to conduct comparative analysis of the performance of wFMFP under different loss functions. We also plan to investigate solutions to improve the performance of wFMFP in parallel computing settings to practical use once the real-time model training is needed.

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Disclosure

The results of this research have been previously published in:

1. Zhou J, Li X, Wang X, Chai Y, Zhang Q. Locally weighted factorization machine with fuzzy partition for elderly readmission prediction. Knowl Based Syst 2022;242:108326.

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